



First Principles Study of the Properties of Cs₂GaAgF₆ Double Halide Perovskite Compound for Optoelectronic and Thermoelectric Applications

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Abstract

This study uses first-principles methods to analyze the structural, electronic, mechanical, thermophysical, optical, and thermoelectric properties of the Cs₂GaAgF₆ double-halide perovskite compound. The results have revealed that the Cs₂GaAgF₆ compound is mechanically and thermodynamically stable and can be potentially synthesized. The calculated band gap of the material was 2.27 eV, 2.41 eV, and 2.54 eV, derived from the local density approximation using Perdew–Zunger functional (LDA-PZ), the generalized gradient approximation using the Wu–Cohen (GGA-WC), and Perdew–Burke–Ernzerhof (GGA-PBE) functionals, respectively. The band gap was improved by using metaGGA functionals, which gave 3.10 eV, 3.15 eV, 3.15 eV, and 4.62 eV for strongly constrained and appropriately normed (SCAN), regularized strongly constrained and appropriately normed (rSCAN), restored-regularized strongly constrained and appropriately normed (r2SCAN), and Tran–Blaha-modified Becke–Johnson (TB-mBJ), respectively. The machine learning (ML) techniques predicted a band gap of 2.68 eV. The mechanical and elastic properties showed that the investigated compound is ductile and elastically anisotropic. Additionally, the optical properties showed excellent performance in the ultraviolet spectrum. Notably, the high absorption coefficients and optical conductivity values across the ultraviolet spectrum underscore the significant potential of the Cs₂GaAgF₆ double-halide perovskite compound for optoelectronic applications. Finally, the Cs₂GaAgF₆ double-halide perovskite compound showed a considerable figure of merit (ZT) value of 0.739 at approximately 600 K, suggesting its suitability for thermoelectric applications.

Keywords Double-halide perovskite · DFT · Thermodynamic stability · Optoelectronics · Thermoelectric applications

1 Introduction

As global energy demand continues to increase with industrial growth and social development, excessive reliance on traditional fossil fuels poses significant challenges, particularly considering escalating ecological concerns [1]. Modern society's unprecedented energy needs have intensified environmental degradation owing to pollution from the byproducts of high-carbon energy use. This growing pressure highlights the urgent need to transition to non-fossil energy sources, steering the world toward a low-carbon future.

Photovoltaics have attracted immense attention as non-fossil energy sources owing to the global abundance of sunlight [2]. Silicon-based photovoltaics have proven to be ideal candidates for non-fossil photovoltaic sources

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because of their advanced technology and high efficiency [3]. Since the theoretical efficiency limit for crystalline silicon photovoltaics is 29.4%, only marginal performance improvements are possible due to intrinsic losses and Auger recombination [4]. Researchers are increasingly focusing on perovskite solar cells (PSCs) as an emerging technology that can deliver high power conversion efficiency (PCE) [5] while maintaining low production costs [6]. PSCs have made remarkable advancements over the past few decades, particularly in their PCE, which has surged to 26.7% [7]. This leap in efficiency has been achieved primarily through the use of lead-based perovskite compounds. However, reliance on lead presents significant environmental and health risks, raising concerns regarding the sustainability of PSC technology [8]. Lead is a toxic metal that can pose serious hazards if not managed properly, particularly in the manufacturing and disposal of solar panels. As the quest for higher efficiencies continues, it is crucial to address these challenges by exploring alternative materials that could replace lead in perovskite formulations while still achieving comparable efficiency.

Lead-free double-halide perovskites, represented by the formula $A_2BB'X_6$, have attracted significant research interest owing to their remarkable properties [9]. Effective perovskite materials have been developed by substituting Pb^{2+} ions with a combination of monovalent B^+ and trivalent B'^{3+} cations [10]. Charef et al. [9] investigated the properties of Na_2AgAsX_6 ($X=Cl, Br$) double-halide perovskite materials using the first-principles method. The desirable band gaps, high absorption in the ultraviolet and visible regions, and good transport properties from this investigation highlighted the potential of these double-halide perovskites as light absorbers for efficient PSCs and thermoelectric applications. The Rb_2AgGaX_6 ($X: Br, Cl$) double-halide perovskites [11] have been found to exhibit band gaps of 1.28 and 2.53 eV and high absorption coefficients of $1.9 \times 10^5 \text{ cm}^{-1}$ and $2.1 \times 10^5 \text{ cm}^{-1}$, desirable for energy applications. The PCEs of Rb_2AgGaX_6 ($X: Br, Cl$) were simulated theoretically under AM 1.5G solar irradiation to be 32.2 and 12%, respectively, further proving their potential for solar-cell device design. Double-halide perovskite compounds A_2AgAsX_6 ($A = K, Rb, Cs; X = Cl, Br, I$) based on arsenic were found to have band gaps ranging from 0.882 to 2.125 eV using the first-principles method [12]. These compounds also exhibited high absorption coefficients in the ultraviolet-visible region, indicating their potential for energy applications.

Double-halide perovskite compounds with Gallium and Silver combinations ($Cs_2AgGa(Cl, Br)_6$) have been studied for optoelectronic and thermoelectric applications using density functional theory (DFT) [13]. Electronic band gaps of about 2.57 eV and 1.42 eV were obtained for $Cs_2AgGaCl_6$

and $Cs_2AgGaBr_6$, respectively. Both compounds exhibited high absorption coefficients (10^5 cm^{-1}) in the ultraviolet and visible regions. A perovskite solar cell based on $Cs_2AgGaBr_6$ was modeled and achieved a high PCE of 32.57%. This shows the potential of Gallium and Silver combinations for realizing efficient double-halide perovskite devices.

The highest reported experimental PCE for lead-free double-halide perovskite solar cells is 6.37% [14]. This was achieved using hydrogenated $Cs-AgBiBr$ perovskite materials. This efficiency is much lower than that achieved using lead-based perovskite materials. Therefore, it is necessary to explore double-halide perovskite materials further to bridge this efficiency gap. In addition, fluoride-based double-halide perovskites have been under-investigated in the literature compared to their iodine, chlorine, and bromine counterparts. Based on the above, we propose a fluoride-based double-halide perovskite compound with a Gallium and Silver combination. No theoretical and experimental studies on the properties of the Cs_2GaAgF_6 material have been reported in the literature, which motivates this study. In particular, a systematic DFT study of the structural, electronic, elastic, mechanical, optical, and thermoelectric properties of Cs_2GaAgF_6 double-halide perovskite compound was conducted using local and semi-local functionals for optoelectronic and thermoelectric applications.

2 Computational Methods

In this investigation, the structural, electronic, elastic, mechanical, optical, and thermoelectric properties of the Cs_2GaAgF_6 double-halide perovskite compound were computed using the plane wave self-consistent field PWscf method in the framework of density functional theory (DFT) [15], as implemented in the Quantum Espresso (QE) code [16]. Ultrasoft pseudopotentials (USPP) [17] and norm-conserving pseudopotentials (NCPP) [18] have been employed to describe the interactions between electrons and ions. USPP was utilized to predict the structural, electronic, elastic, mechanical, and thermoelectric properties, whereas NCPP was used to predict the optical properties. This study employs local and semi-local approximations. These include the local density approximation (LDA) [19] and the generalized gradient approximation (GGA), utilizing the Perdew–Zunger (PZ), Perdew–Burke–Ernzerhof (PBE) [20], and Wu–Cohen (WC) [21] functional schemes to account for exchange-correlation effects. The strongly constrained and appropriately normed (SCAN), regularized strongly constrained and appropriately normed (rSCAN), restored-regularized strongly constrained and appropriately normed (r2SCAN) [22, 23, 24], and Tran–Blaha-modified Becke–Johnson (TB-mBJ) [25] functionals were further

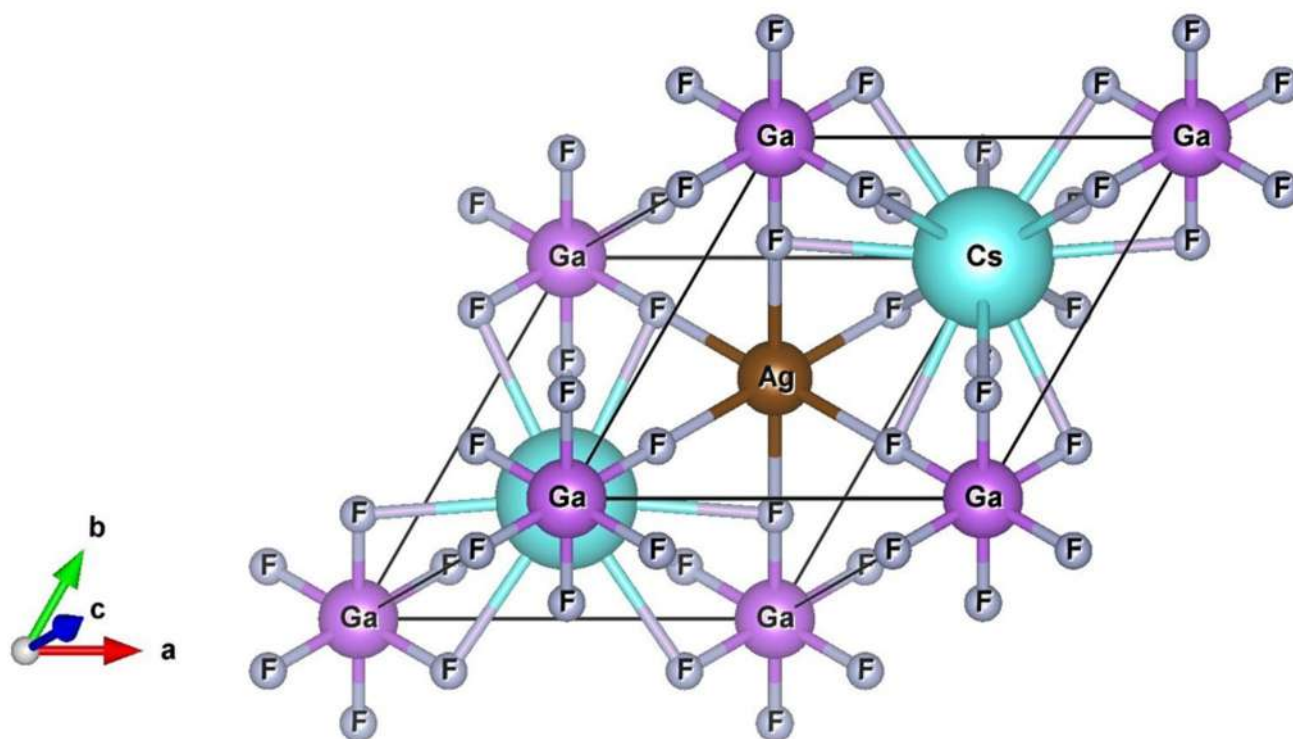


Fig. 1 Primitive crystal structure of $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound

Table 1 Ground state structural properties of $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound

	GGA-PBE	GGA-WC	LDA
Lattice parameter a_0 (Å)	9.025	8.850	8.654
Bulk modulus B_0 (GPa)	13.97	15.90	18.79
Equilibrium volume V_0 (Å ³)	734.91	693.75	647.42
Energy of formation ΔH_f (Ry)	-1.77	-1.78	-1.88

used to improve the accuracy of the band gaps because LDA and GGA tend to underestimate them [26, 27]. Other than DFT, the aflow machine learning online tool (AFLOW-ML) accessed at www.aflowlib.org was used to predict the band gap of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound. The authors of the ML model and its accuracy and error margins are reported in the literature [28, 29, 30, 31]. The first irreducible Brillouin Zone sampling was performed using a Monkhorst–Pack sampling scheme with a converged k-point grid set at $9 \times 9 \times 9$ with a 1 offset. A converged kinetic energy cutoff of 150 Rydberg and a charge density cutoff of 1200 Rydberg were applied for the calculations. A denser k-point grid of $12 \times 12 \times 12$ was used for the non-self-consistent field calculations. A geometry optimization step was performed to calculate the ground-state structural properties. This was achieved by minimizing the total energy with respect to the cell dimensions, followed by fitting these values to the Birch–Murnaghan equation of state [32] to obtain the ground-state crystal structure parameters.

Further optimization was done through the variable cell relaxation to relax the atoms by employing the Broyden–Fletcher–Goldfarb–Shanno (BFGS) algorithm. The crystal structure of $\text{Cs}_2\text{GaAgF}_6$ was visualized using VESTA software. All other electronic, elastic, mechanical, optical, and thermoelectric properties were predicted under the optimized conditions.

3 Results and Discussion

3.1 Structural Properties

The $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound crystallizes in a cubic structure with the $Fm\bar{3}m$ (225) space group [33]. Figure 1 shows the primitive crystal structure. The Cs atoms are bonded to twelve equivalent F atoms to form a Cs–F bond with a length of 3.18 Å, Ag is bonded to six equivalent F atoms to form an Ag–F bond with a length of 2.53 Å, whereas Ga is bonded to six equivalent F atoms to form a Ga–F bond with a length of 1.94 Å.

The geometry optimization of the total energy versus different unit cell volumes results in values that are fitted into the Birch–Murnaghan equation of state [32] to determine the ground-state structural properties, which are presented in Table 1. Using both LDA and GGA, the value of the equilibrium lattice parameter, a_0 , ranged from 8.654 to 9.025 Å.

The bulk modulus describes the resistance against changes in volume due to the applied external pressure [34]. A large bulk modulus indicates a hard material. The computed B_0 values using the GGA and LDA methods range between 13.97 and 18.79 GPa. Compared with the bulk moduli of representative soft materials (NaSbS₂ polymorphs) of 20.60 GPa [35], Cs₂GaAgF₆ demonstrates a slightly lower bulk modulus, placing it as a relatively soft material.

The energy of formation (ΔH_f) was calculated using Eq. (1) [36].

$$\Delta H_f = E_{\text{Cs}_2\text{GaAgF}_6} - (2E_{\text{Cs}} + E_{\text{Ga}} + E_{\text{Ag}} + 6E_{\text{F}}) \quad (1)$$

where $E_{\text{Cs}_2\text{GaAgF}_6}$ is the total energy of Cs₂GaAgF₆ double-halide perovskite compound while E_{Cs} , E_{Ga} , E_{Ag} , and E_{F} are total energies of isolated Cs, Ga, Ag, and F atoms, respectively.

The values of ΔH_f calculated using both local and semi-local functionals were negative, indicating that the Cs₂GaAgF₆ double-halide perovskite compound is thermodynamically stable [36]. Further, the dynamic stability of the Cs₂GaAgF₆ double-halide perovskite compound was

studied by computing phonon dispersions. This was performed using a linear response method based on perturbation density functional theory (DFPT) [37], in which the force constants, interatomic dynamical matrices, and the lattice dynamics are determined from the nuclear geometry and electronic charges [37]. The `thermos_pw` code of Quantum Espresso, and a q-points grid of $4 \times 4 \times 4$ in the crystal lattice, was used for phonon dispersion calculations. As observed in Fig. 2, the phonon dispersion curve of the Cs₂GaAgF₆ double-halide perovskite compound has positive frequency modes, proving its dynamical stability [38]. The thermodynamic stability of the Cs₂GaAgF₆ compound indicates its potential synthesizability. While no experimental synthesis was attempted in this work, similar wide band gap double-halide perovskites such as [Cs₂XBiCl₆ (X=Al, Ag) [39, 40] have been successfully synthesized, supporting the feasibility of synthesizing Cs₂GaAgF₆ under suitable conditions.

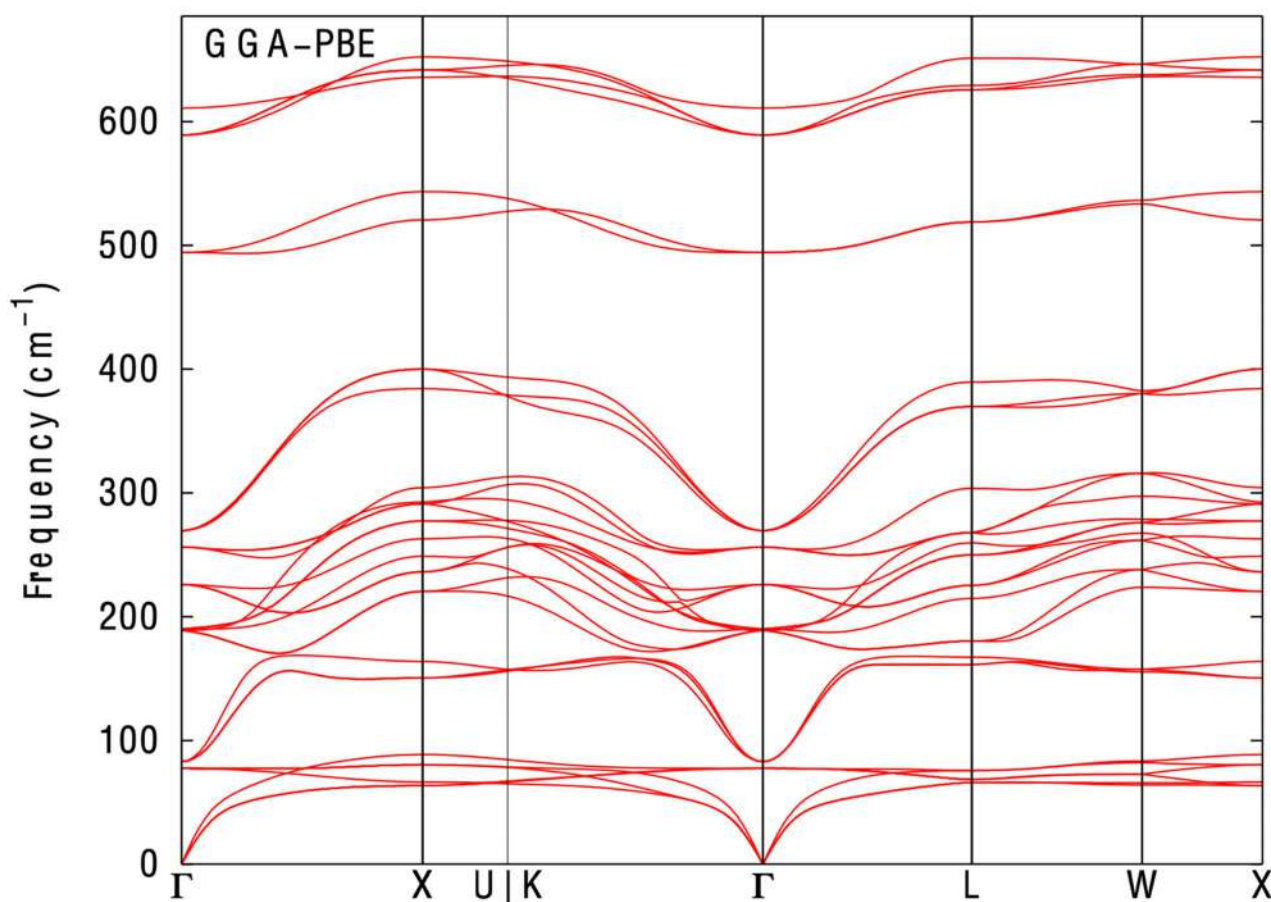


Fig. 2 Phonon dispersion curve of Cs₂GaAgF₆ double-halide perovskite compound

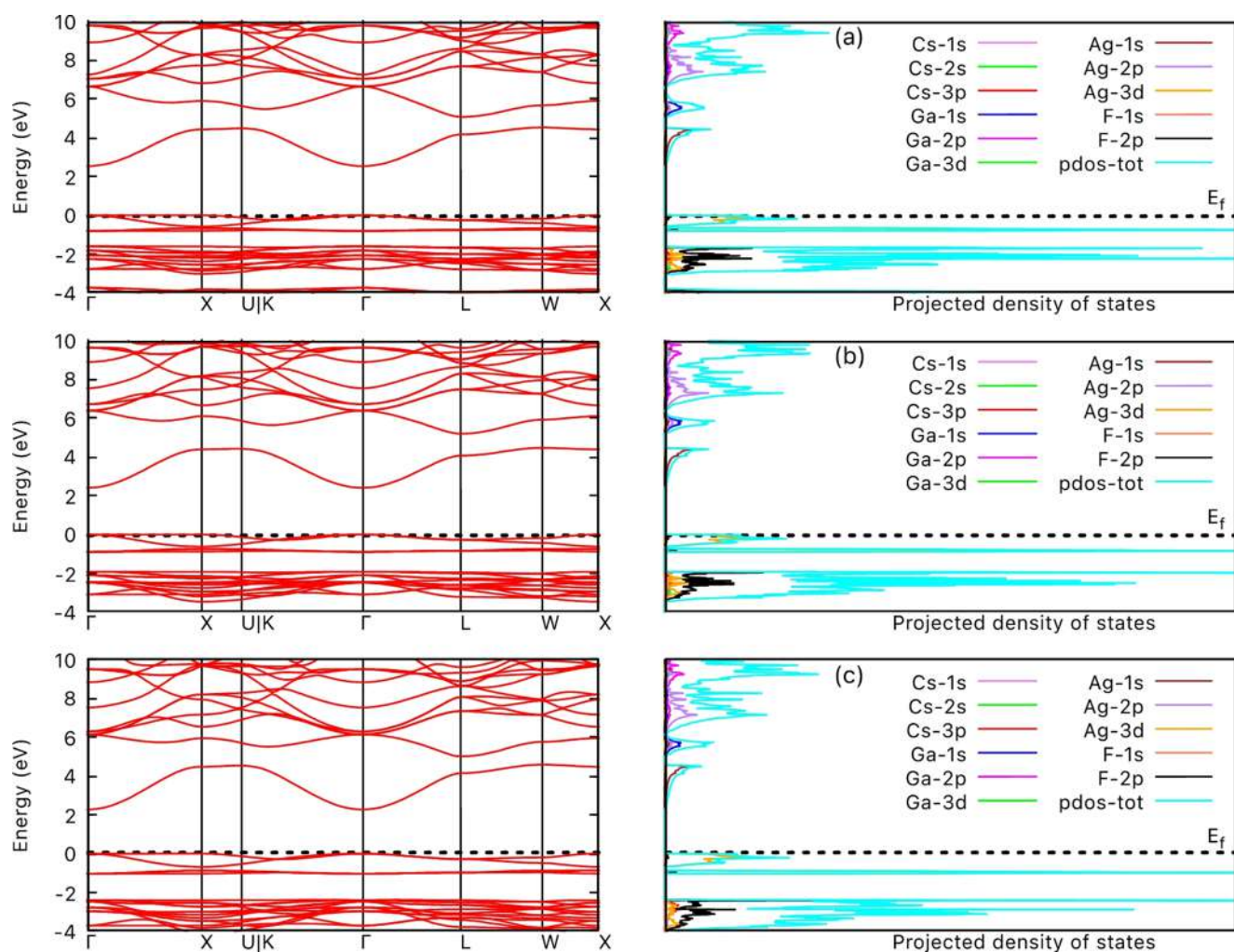


Fig. 3 The band structure and projected density of states of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound computed using **a** GGA-PBE, **b** GGA-WC, and **c** LDA approximations

3.2 Electronic Properties

The electronic band structure and projected density of states are effective for determining the nature of a material. An overlap of the electronic states in the valence and conduction bands at the Fermi level implies that the material under investigation is a conductor; otherwise, it is a semiconductor [41]. The electronic states in Fig. 3 show a separation gap between the valence and conduction bands, suggesting that the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound is a semiconductor. The valence band maxima and the conduction band minima lie on the same/different high symmetry points, Γ – Γ and X – Γ , in the first Brillouin zone, implying that the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound is a direct/indirect band gap semiconductor [42]. Figure 3 shows that the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound has wide band gaps of 2.54, 2.41, and 2.27 eV using GGA-PBE, GGA-WC, and LDA approximations. LDA and

Table 2 The electronic band gaps of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound calculated using different approximations

Methods	Band gaps (eV)
GGA-PBE	2.54
GGA-WC	2.41
LDA	2.27
SCAN	3.10
RSCAN	3.15
R2SCAN	3.15
TB-mBJ	4.62
AFLOW-ML	2.68

GGA approximations are known to understate the electronic band gaps of semiconducting materials [41]. Therefore, the SCAN, RSCAN, R2SCAN, and TB-mBJ functionals were utilized to improve accuracy. As shown in Table 2, the band gap of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound increased to 3.1, 3.15, 3.15, and 4.62 eV by utilizing the SCAN, RSCAN, R2SCAN, and TB-mBJ functionals,

respectively. These wide band gap values are closely related to the ones reported for other double-halide perovskite compounds ($\text{Cs}_2\text{AgGaCl}_6$, $\text{Cs}_2\text{NaXCl}_6$ ($X=\text{In, La, Sc, Y}$), $\text{Rb}_2\text{NaTiZ}_6$ ($Z=\text{Cl, Br, and I}$), and Cs_2YAgX_6 ($X=\text{Cl, Br, I}$) with similar stoichiometry [13, 43, 44, 45]. The AFLOW-ML tool predicted the band gap of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound to be 2.68 eV. This value is closely related to the values obtained from DFT methods, suggesting the reliability of DFT methods in predicting electronic band gaps. The wide band gaps obtained for the $\text{Cs}_2\text{GaAgF}_6$ semiconductor material render it suitable for optoelectronic applications [46]. It was further observed from the projected density of states in Fig. 3 that the $\text{F}2p$ and $\text{Ag}3d$ states dominated the formation of the valence band. In contrast, the $\text{Ga}2p$, $\text{Ag}2p$, $\text{Ga}s$, and $\text{Ag}s$ states significantly contributed to the formation of the conduction band. All other unaccounted states contributed insignificantly to the formation of the valence and conduction bands.

3.3 Elastic and Mechanical Properties

The elastic properties/constants (C_{ij}) of the $\text{Cs}_2\text{GaAgF}_6$ compound were computed using the `thermos_pw` code in Quantum Espresso. The cubic crystal system features three independent elastic constants, namely C_{11} , C_{12} , and C_{44} [47]. The Born stability criteria for the cubic crystal system are $C_{11}-C_{12}>0$, $C_{11}+2C_{12}>0$, and $C_{44}>0$ [47]. The computed elastic constants for the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound adhere to the mentioned Born stability criteria, symbolizing mechanical stability. From these elastic constants, other mechanical properties, including bulk modulus B , Young's modulus E , Shear modulus G , and Poisson's ratio ν , are deduced using the Voigt-Reuss-Hill (VRH) averaging scheme [48]. The Voigt and Reuss constants are represented by Eqs. (2) and (3), while the Hill's average of the Voigt and Reuss schemes for a cubic crystal system is given by Eq. (4) [49].

$$B_V = \frac{(C_{11} + 2C_{12})}{3}; \quad G_V = \frac{(C_{11} - C_{12} + 3C_{44})}{5} \quad (2)$$

$$B_V = B_R; \quad G_R = \frac{5(C_{11} - C_{12})C_{44}}{4C_{44} + 3(C_{11} - C_{12})} \quad (3)$$

$$B = \frac{B_V + B_R}{2}; \quad G = \frac{G_V + G_R}{2} \quad (4)$$

The Young's modulus and Poisson's ratio are calculated using Eq. (5).

$$E = \frac{9BG}{3B + G}; \quad \nu = \frac{3B - 2G}{2(3B + G)} \quad (5)$$

The B , E , and G describe the ability of a material to resist volume deformation, uniaxial tension, and plastic deformation, respectively [50]. The B/G and ν ratio investigates the materials' ductile and brittle nature. A B/G ratio greater than 1.75 denotes a ductile nature; otherwise, a brittle nature [51]. Moreover, a material is said to be brittle if $\nu < 0.26$ and ductile if $\nu > 0.26$ [51]. The obtained B/G and ν values in Table 3 show that the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound exhibits a ductile nature. The elastic anisotropy (A) in cubic crystal systems is characterized by Eq. (6) [52]. The A value of 1 demonstrates that a material is elastically isotropic; any deviations prove anisotropy. Our calculations indicate that the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound is elastically anisotropic.

$$A = \frac{2C_{44}}{C_{11} - C_{12}} \quad (6)$$

To further estimate the mechanical anisotropy of the $\text{Cs}_2\text{GaAgF}_6$ compound, the 3D spatial dependences of the Young's modulus and Shear modulus along the x , y , and z planes were deduced from the elastic constants using the ELATE: Elastic matrix tensor analysis [53] software, as shown in Fig. 4. A material is termed isotropic if the 3D distribution maps adopt a spherical shape; otherwise, it is anisotropic [54]. According to Fig. 4, the distribution maps show a deviation from the spherical shape, suggesting anisotropic behavior.

3.4 Optical Properties

To determine the potential application of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound in optoelectronics, its optical properties were investigated by computing the complex dielectric wave function. The GGA-PBE approximation was used as a representative method to compute the complex dielectric wave function. The complex dielectric wave function describes the electron response in a material and is represented by Eq. (7) [55, 56].

Table 3 The elastic constants in GPa and mechanical properties of the $\text{Cs}_2\text{GaAgF}_6$ cubic crystal structure

	GGA-PBE
C_{11}	45.56
C_{12}	35.47
C_{44}	16.08
B (GPa)	38.83
E (GPa)	27.89
G (GPa)	10.12
B/G	3.84
ν	0.38
A	3.19

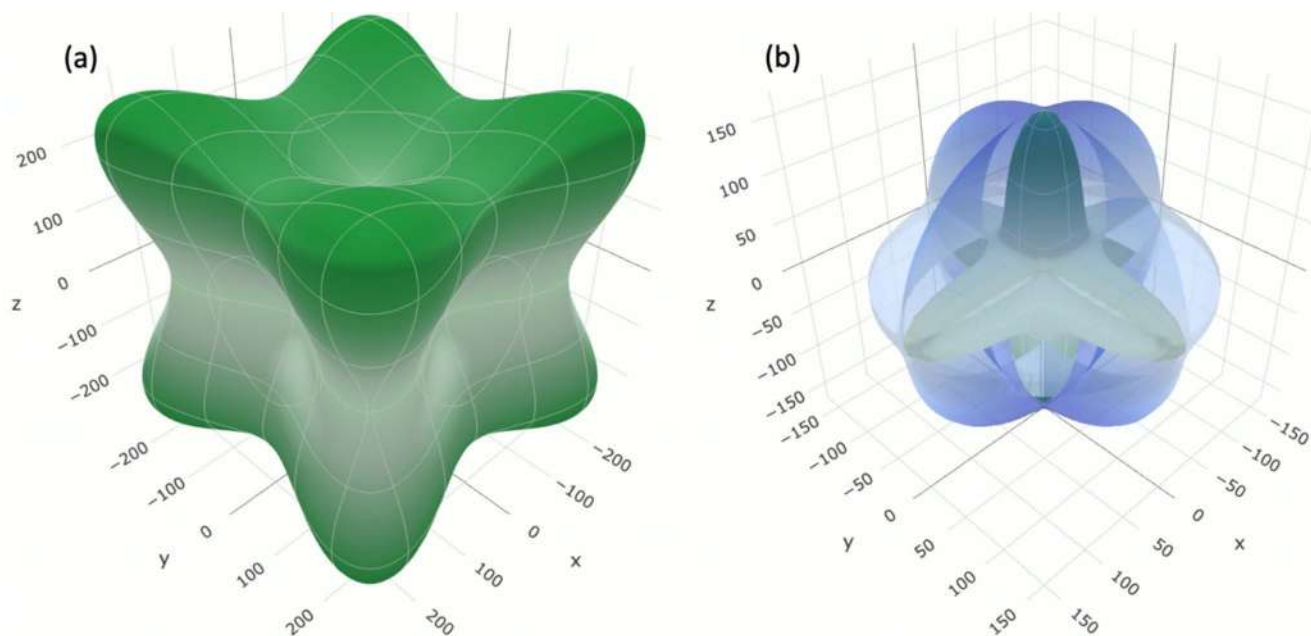


Fig. 4 Three-dimensional distribution maps of **a** Young's modulus and **b** shear modulus of $\text{Cs}_2\text{GaAgF}_6$ lead-free double perovskite compound along the x, y, and z planes

$$\epsilon(\omega) = \epsilon_1(\omega) + i\epsilon_2(\omega) \quad (7)$$

where $\epsilon_1(\omega)$ and $\epsilon_2(\omega)$ are the real and imaginary components of the dielectric wave function. The other optical properties, such as the refractive index $n(\omega)$, absorption coefficient $\alpha(\omega)$, optical conductivity $\sigma(\omega)$, extinction coefficient $K(\omega)$, reflectivity $R(\omega)$, and energy loss function $L(\omega)$ are computed using the equations reported in the literature [57].

The imaginary component $\epsilon_2(\omega)$ represents the phenomenon of light absorption, which occurs when the light frequency exceeds a specific threshold limit [58]. The computed band gap of $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound using GGA-PBE approximation is consistent with the absorption onsets of $\epsilon_2(\omega)$ spectra in Fig. 5a. The observed peaks in $\epsilon_2(\omega)$ spectra are attributed to the transition of the electronic states from the valence band to the conduction band. The $\epsilon_2(\omega)$ curves in Fig. 5a attain their maximum at 15.4 eV. Thereafter, the $\epsilon_2(\omega)$ spectra begin to decrease with an increase in energy. The $\epsilon_1(\omega)$ describes the polarization and dispersion of the light from the lattice [58]. The $\epsilon_1(\omega)$ spectra in Fig. 5b increase from zero energy and attain a maximum of 3.6 at 5.8 eV. The energy transmission continues until the $\epsilon_1(\omega)$ spectra becomes negative at 15.4–16.6 eV. At this point, the incident photon energies are assumed to be fully attenuated [59], and the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound exhibits metallic behavior [60]. These negative values translate to limited transmission, reflection, and optical energy losses, suggesting a material's suitability as an insulator within this energy range [61]. The

zero-frequency limit, $\epsilon_1(0)$, also called the static point, is correlated with the refractive index, $n(0)$, as the square root of $\epsilon_1(\omega)$ at energy (eV)=0. The static value obtained for the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound is 2.72, as seen in Fig. 5b. The refractive index describes the bending of light traveling through a material. The $n(0)$ value of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound observed in Fig. 5c is 1.65. The $n(\omega)$ spectra in Fig. 5c is observed to be high in the 4.6–15 eV energy regions and thereafter decrease. The $\alpha(\omega)$ spectra demonstrate the depth of light of a specific wavelength that can penetrate the material before complete absorption [62]. As shown in Fig. 5d, the $\alpha(\omega)$ spectra increase gradually through the visible region and peak in the ultraviolet (UV) region, reaching a maximum at 15.6 eV. The high optical absorption of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound in the ultraviolet region highlights its potential utility in UV photodetectors [63] and tandem solar cell configurations [64], where UV absorption contributes to the overall device efficiency.

The $\sigma(\omega)$ is directly correlated to the $\alpha(\omega)$. As shown in Fig. 6a, the $\sigma(\omega)$ spectra pattern matches that of $\alpha(\omega)$ in Fig. 5d. The $\sigma(\omega)$ spectra increase with increasing energy, reaching a maximum of 55,810 S/m in the ultraviolet region at 16.3 eV. These results show that the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound is a good optical conductor that can be used in optoelectronics. The $k(\omega)$ describes the amount of absorbed energy by a material. The threshold energy of $k(\omega)$ for the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound is determined to be 2.5 eV in Fig. 6b. The $k(\omega)$

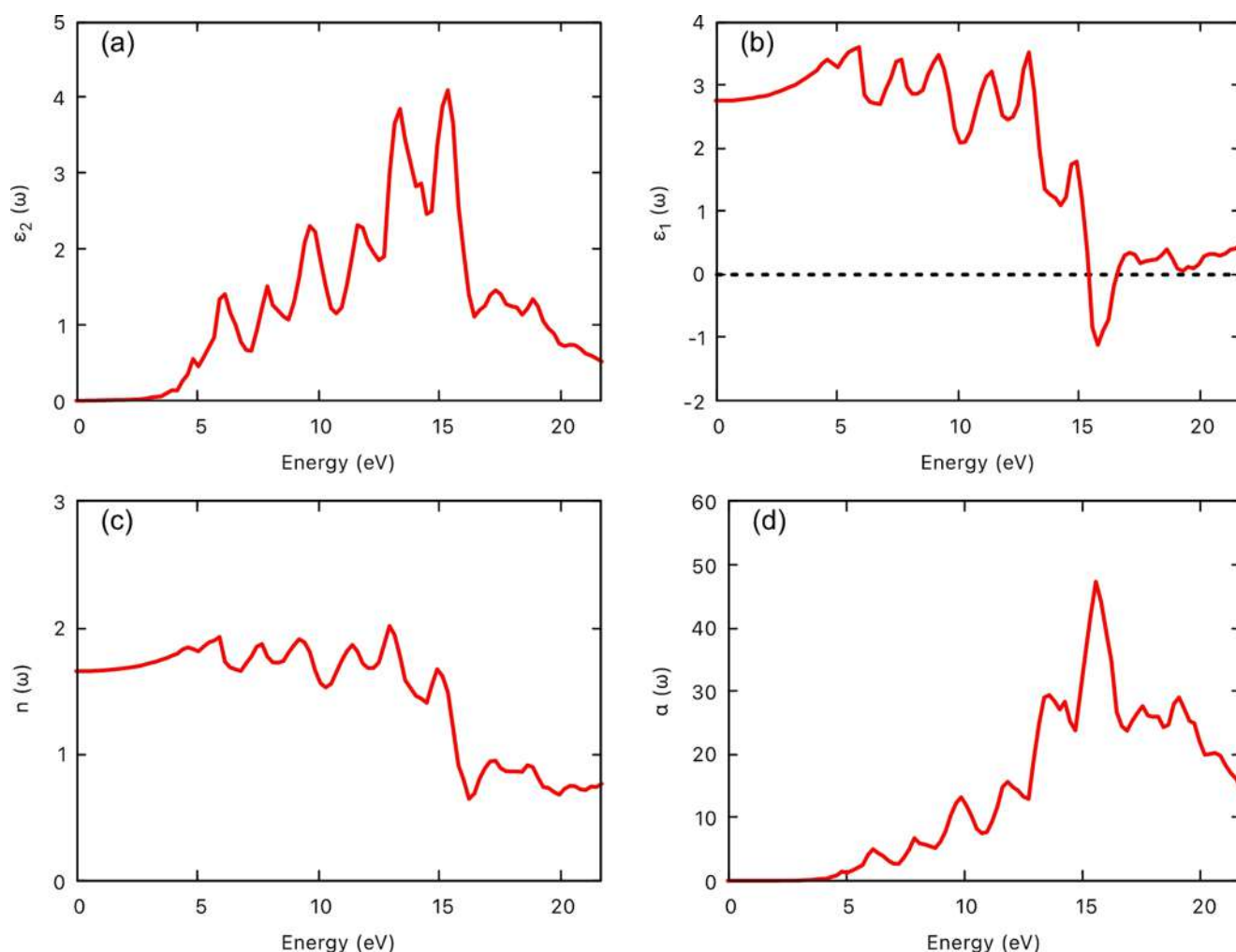


Fig. 5 **a** Imaginary dielectric constant, **b** real dielectric constant, **c** refractive index, and **d** absorption coefficient of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound

spectra in Fig. 6b increase strongly with increasing energy and attain a maximum in the UV region. This reflects the substantial absorption of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite. The $R(\omega)$ describes the optical response of the material surface [65]. The static reflectivity $R(0)$ of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound is 0.06 as seen in Fig. 6c. The $R(\omega)$ spectra are observed to increase gradually, attaining a maximum value at 15.9 eV and thereafter gradually decreasing. The $L(\omega)$ defines the energy loss by electrons passing through the material [65]. As shown in Fig. 6d, there is a low absorption in the 0–15 eV energy region. Thereafter, a major absorption occurrence is observed. These obtained and observed optical properties are consistent with those reported for other wide band gap halide-based double perovskite compounds [43, 44, 45, 62].

3.5 Thermoelectric Properties

The thermoelectric properties describe the material's ability to generate electrical energy from heat [66]. The transport properties, including Seebeck coefficient (S), electrical conductivity (σ/τ), and electronic thermal conductivity (k_e/τ), were computed using the BoltzTraP code [67] at a temperature (T) ranging from 50 to 800 K (see Fig. 7). The S for $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound exhibits a decreasing trend with temperature, starting at 188 $\mu\text{V}/\text{K}$ at 50 K and gradually reducing to 149 $\mu\text{V}/\text{K}$ at 800 K as observed in Fig. 7a. This behavior aligns with the general trend observed in many thermoelectric materials, where increasing the carrier concentration at higher temperatures reduces the Seebeck coefficient owing to the inverse relationship between S and charge carrier density. The σ/τ in Fig. 7b increases steadily with temperature, reaching 1.35×10^{19} S/m at 800 K. This increase suggests that $\text{Cs}_2\text{GaAgF}_6$ follows a semiconductor-like behavior, where

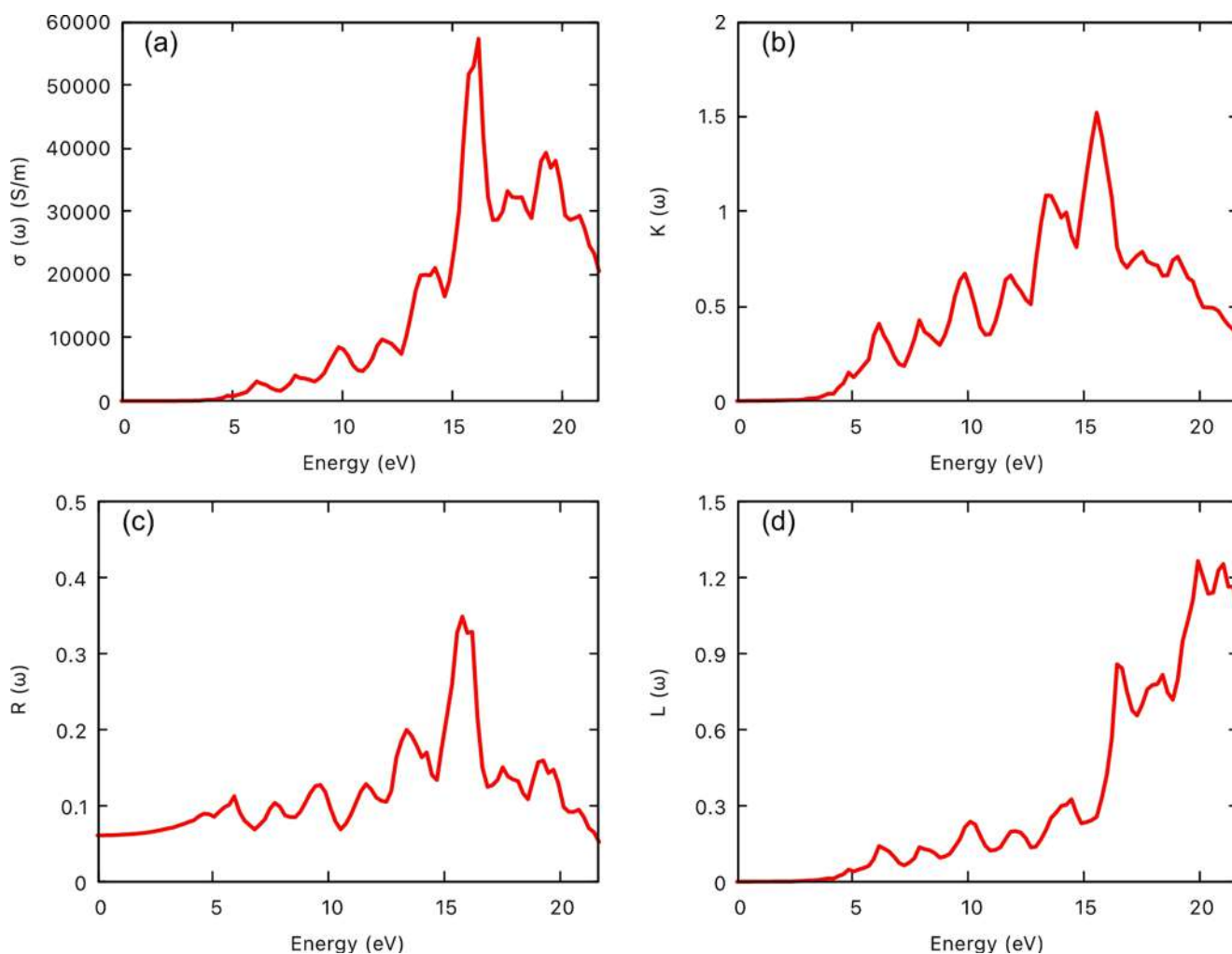


Fig. 6 **a** Optical conductivity, **b** extinction coefficient, **c** reflectivity spectra, and **d** energy loss function of $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound

higher temperatures enhance carrier excitation, thus improving conductivity. Such behavior is crucial for an efficient thermoelectric material, as higher conductivity minimizes the Joule heating losses. The k_e/τ in Fig. 7c rises significantly with temperature, from 4.47×10^{12} W/mK at 50 K to 3.28×10^{14} W/mK at 800 K. This increase correlates with the growing electrical conductivity, as dictated by the Wiedemann-Franz law. However, the increasing electronic thermal conductivity should be balanced by a low lattice thermal conductivity (k_l) for optimal thermoelectric performance. The k_l was computed using the phono3py code [68] and the Quantum Espresso code. The k_l shown in Fig. 7d exhibits a decreasing trend with increasing temperature, dropping from 1.46×10^7 W/mK at 50 K to 1.22×10^6 W/mK at 800 K. The obtained k_l values are within a reasonable range as compared to other related double perovskite materials [A_2GeSnF_6 (A=K, Rb, Cs)] whose values have been reported to be in the range 5.53×10^{13} to 0.24×10^{13} W/mKs, 5.83×10^{13} to 0.53×10^{13} W/mKs, and 2.91×10^{13} to

0.122×10^{13} W/mKs, respectively [49]. This reduction indicates enhanced phonon scattering at higher temperatures, a desirable feature of thermoelectric materials for suppressing heat dissipation and improving the figure of merit (ZT). The ZT was calculated from the computed transport properties using Eq. (8) [69].

$$ZT = \frac{S^2 \sigma T}{k_e + k_l} \quad (8)$$

As observed in Fig. 7e, the dimensionless ZT improves with temperature, peaking at 0.739 at approximately 600 K, and maintaining high values thereafter. This peak reflects an optimal operating temperature window around 600 K, where the trade-off between the decreasing Seebeck coefficient, increasing electrical conductivity, and decreasing lattice thermal conductivity yields the optimal thermoelectric efficiency. This highlights the suitability of $\text{Cs}_2\text{GaAgF}_6$ for medium-high temperature thermoelectric applications.

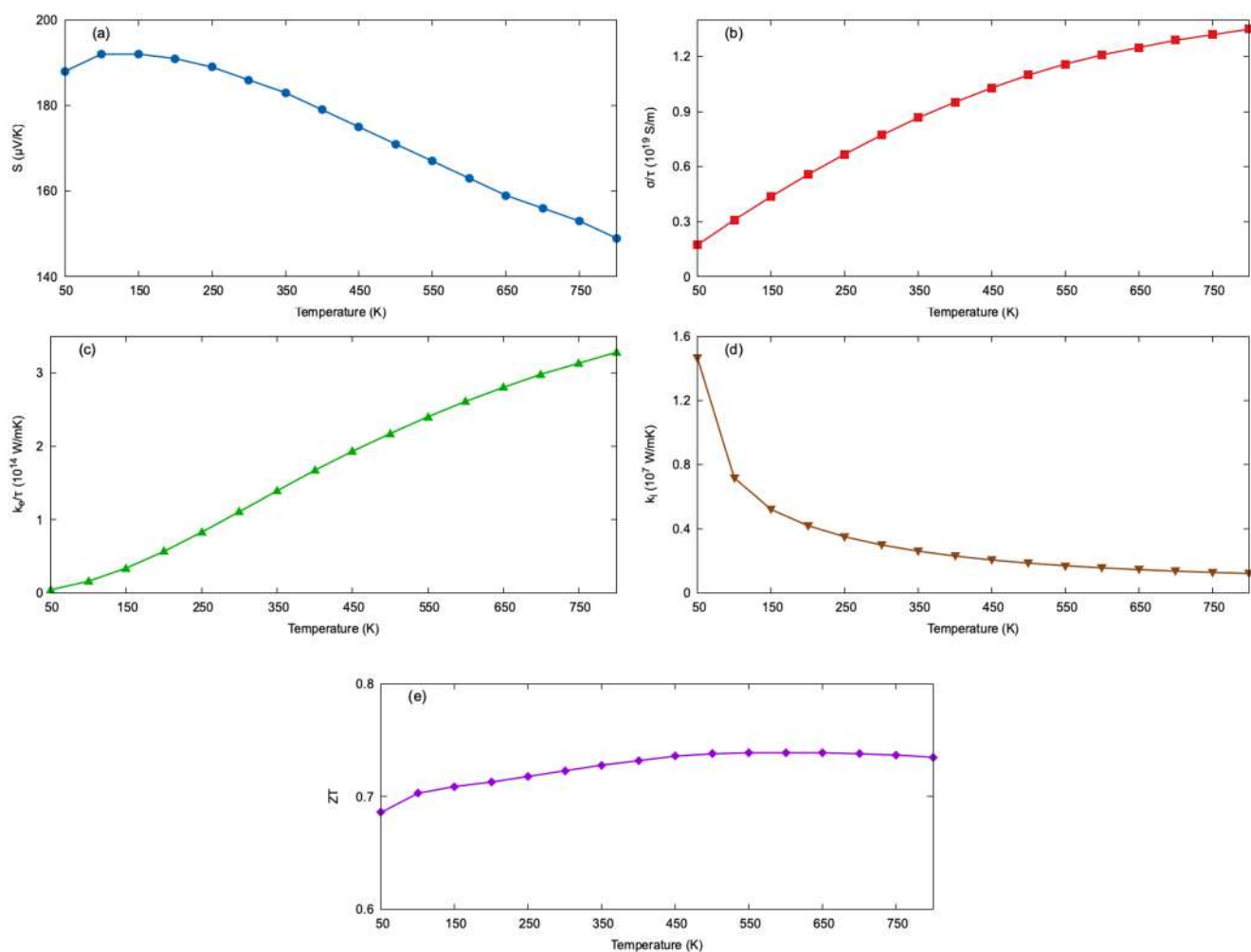


Fig. 7 **a** The Seebeck coefficient (S), **b** electrical conductivity (σ/τ), **c** electronic thermal conductivity (k_e/τ), **d** lattice thermal conductivity (k_l), and **e** figure of merit (ZT) of the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound computed using the GGA-PBE approximation

4 Conclusion

This work examines the structural, electronic, elastic, mechanical, optical, and thermoelectric properties of $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound for optoelectronic and thermoelectric applications. The structural, thermodynamic, and mechanical stability of the studied compound is confirmed through nonimaginary phonon frequency modes, negative formation energies, and elastic constants, respectively. The $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound is found to be ductile and elastically anisotropic from mechanical and elastic calculations. The wide band gaps ranging from 2.27 eV to 4.62 eV were obtained using different approximation methods. The $\text{F}2p$ and $\text{Ag}3d$ states primarily contribute to the formation of the valence band, whereas the $\text{Ga}2p$, $\text{Ag}2p$, $\text{Ga}1s$, and $\text{Ag}1s$ states significantly influence the formation of the conduction band. Optical absorption bands were observed in the ultraviolet region, which is potentially crucial for optoelectronic

applications. Additionally, the $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound showed significant thermoelectric performance with a high ZT value of 0.739 at approximately 600 K, indicating its potential as a thermoelectric material. This work thus provides theoretical insights that may guide and motivate future experimental synthesis and characterization of $\text{Cs}_2\text{GaAgF}_6$ double-halide perovskite compound.

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Declarations

Conflict of interest The authors have no conflicts of interest to declare that are relevant to the content of this article.

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